

Table 1b, Charge and Current Densities
for the Metrics of Table 1a.
Charge and Current Densities

Metric	Charge and Current Densities
Minkowski	$J^0 = 0, J_r = 0, J_\theta = 0, J_\phi = 0$
Schwarzschild	$J^0 = 0, J_r = 0, J_\theta = 0, J_\phi = 0$
Gödel	$J^0 = 0, J_r = 0, J_\theta = 0, J_\phi = 0$
Kasner	$J^0 = 0, J_r = 0, J_\theta = 0, J_\phi = 0$
Cotler Type 0 ₀	$J^0 = 0, J_r = 0, J_\theta = 0, J_\phi = 0$
- Cotler/ Original Minkowski	$J^0 = 0, J_r = 0, J_\theta = 0, J_\phi = 0$
Cotler/Minkowski	$J^0 = 0, J_r = 0, J_\theta = 0, J_\phi = 0$
FLRW	$J^0 = -3\phi \ddot{a} = 4\pi \phi G(\rho + 3p),$ $J_r = -\frac{A^{(0)}}{\mu_0} \left(\frac{2}{a^4} (k + \ddot{a}^2)(kr^2 - 1) + \frac{\ddot{a}}{a^3} (kr^2 - 1) \right),$ $J_\theta = \sin^2 \theta J_\phi = \frac{A^{(0)}}{\mu_0} \left(\frac{2}{a^4 r^2} (k + \ddot{a}^2) + \frac{\ddot{a}}{a^3 r^2} \right).$
Cotler's General	$J^0 = -\frac{\ddot{C}}{4ABC^2} \phi,$ $J_r = -\frac{A^{(0)}}{\mu_0} \left(\frac{5C\ddot{C} - 4\dot{C}^2}{4B^2C^3} \right),$ $J_\theta = \frac{A^{(0)}}{\mu_0} \left(\frac{2BC^{1/2} - \ddot{C}}{2BC^{5/2}} \right),$ $J_\phi = \frac{J_\theta}{\sin^2 \theta},$ <p>where $\ddot{C} = \frac{d^2 C}{dr^2}, \dot{C} = \frac{dC}{dr}.$</p>

Table 1b Continued.

Coupled with
Defined $c(r)$

Here $c(r) = (|r - r_0|^n + d^n)^{2/n}$
Finite charge and current densities. In the
special case:

$$r_0 = 0, \quad d = 0$$

The following are obtained.

$$J^0 = -\frac{\phi}{2r^4 AB}$$

$$J_r = \frac{A^{(0)}}{\mu_0} \cdot \frac{3}{2r^4 B^2}$$

$$J_\theta = \sin^2 \theta \cdot J_\phi = \frac{A^{(0)}}{\mu_0} \left(\frac{r^2 B - |r|}{r^6 B} \right)$$

Static
de Sitter

$$J^0 = -\frac{3\phi}{r^2 - d^2}$$

$$J_r = -\frac{A^{(0)}}{\mu_0} \left(\frac{3r^2 - 3d^2}{d^4} \right)$$

$$J_\theta = \sin^2 \theta \cdot J_\phi = \frac{A^{(0)}}{\mu_0} \cdot \frac{3}{d^2 r^2}$$

Wormhole
Metric

$$ds^2 = -c^2 dt^2 + dr^2 + (l^2 + k^2)(d\theta^2 + \sin^2 \theta d\phi^2).$$

Here:

$$J^0 = 0,$$

$$J_r = -\frac{A^{(0)}}{\mu_0} \left(\frac{2k^2}{(l^2 + k^2)^2} \right),$$

$$J_\theta = J_\phi = 0.$$

Alcubierre,
Kerr and
Charged Kerr

Here $R \wedge \eta \neq 0$ (?)
so these metrics do not correctly obey
the Ricci cyclic equation, usually known
as the first Bianchi identity.

Table 1b Continued

General Spherical Metric

$$ds^2 = -c^2 dt^2 e^{2\alpha} + e^{2\beta} dr^2 + d\theta^2 + \sin^2 \theta d\phi^2,$$

Here:

$$J^0 = \rho \left(e^{-2\beta - 4\alpha} \left(\left(e^{2\beta} \frac{d^2 \beta}{dt^2} \right) + e^{2\beta} \left(\frac{d\beta}{dt} \right)^2 \right. \right. \\ \left. \left. - \frac{d\alpha}{dt} e^{2\beta} \frac{d\beta}{dt} + e^{2\alpha} \frac{d\alpha}{dr} \frac{d\beta}{dr} - e^{2\alpha} \frac{d^2 \alpha}{dr^2} \right) r \right. \\ \left. - 2 e^{2\alpha} \frac{d\alpha}{dr} \right) / r,$$

$$J_r = \frac{A^{(0)}}{\mu_0} \left(e^{-4\beta - 2\alpha} \left(\left(e^{2\beta} \frac{d^2 \beta}{dt^2} + e^{2\beta} \left(\frac{d\beta}{dt} \right)^2 \right. \right. \right. \\ \left. \left. - \frac{d\alpha}{dt} e^{2\beta} \frac{d\beta}{dt} + e^{2\alpha} \frac{d\alpha}{dr} \frac{d\beta}{dr} \right. \right. \\ \left. \left. - e^{2\alpha} \frac{d^2 \alpha}{dr^2} - e^{2\alpha} \left(\frac{d\alpha}{dr} \right)^2 \right) r \right. \\ \left. + 2 e^{2\alpha} \frac{d\beta}{dr} \right) / r,$$

$$J_\theta = J_\phi \sin^2 \theta \\ = \frac{A^{(0)}}{\mu_0} \frac{1}{r^4} e^{-2\beta} \left(\left(\frac{d\beta}{dr} - \frac{d\alpha}{dr} \right) r \right. \\ \left. + e^{2\beta} - 1 \right).$$

The charge and current densities are not-zero in general.