

79(3): (under gravitation for the ECE Wave Equation.)

Consider the ECE wave equation:

$$\square \phi = R \phi, \quad (1)$$

which can be deduced from the tetrad postulate of Cartan geometry. More generally:

$$\square A^\mu = R A^\mu \quad (2)$$

where A^μ is the four potential

$$A^\mu = \left(\frac{\phi}{c}, \underline{A} \right) \quad (3)$$

Eqs. (1) and (2) are special cases of:

$$\square A^\alpha_\mu = R A^\alpha_\mu \quad (4)$$

here

$$A^\alpha_\mu = A^{(0)} q^\alpha_\mu \quad (5)$$

where q^α_μ is the Cartan tetrad. The scalar curvature R has units of m^{-2} .

Eq. (1) is:

$$\frac{1}{c^2} \frac{\partial^2 \phi}{\partial t^2} - \nabla^2 \phi = R \phi \quad (6)$$

and has the solution:

$$\phi = \phi_0 \exp(i(\omega t - \underline{\kappa} \cdot \underline{r})) \quad (7)$$

in which:

$$\frac{\omega^2}{c^2} - \kappa^2 = R \quad (8)$$

Using:

$$E = \hbar \omega, \quad p = \hbar \underline{\kappa} \quad (9)$$

and

$$R = \left(\frac{p}{mc} \right)^2 \quad (10)$$

Eq. (8) becomes the relativistic energy equation:

$$E^2 = c^2 p^2 + m^2 c^4 \quad (11)$$

i.e

$$E = \gamma mc^2 \quad (12)$$

where

$$\gamma = \left(1 - \frac{v_0^2}{c^2} \right)^{-1/2} \quad (13)$$

is the Lorentz factor. Here \underline{v}_0 is the Newtonian velocity in the observer frame.

If ϕ is assumed to have no time dependence,

then

$$(\nabla^2 + R)\phi = 0 \quad (14)$$

where

$$\phi = \phi_0 \exp(-i\underline{\kappa} \cdot \underline{r}) \quad (15)$$

Euler Bernoulli resonance is produced from (14) if:

$$(\nabla^2 + R)\phi = A \cos \underline{\kappa} \cdot \underline{r} \quad (16)$$

which

$$R = \kappa_0^2 \quad (17)$$

The solution of Eq. (16) in one dimension Z is the solution of

$$\frac{\partial^2 \phi}{\partial Z^2} + \kappa_0^2 \phi = A \cos \kappa Z \quad (18)$$

and is:

$$\phi = \frac{A \cos k_z z}{k_0^2 - k^2} \quad (19)$$

At resonance:

$$k = k_0 \quad (20)$$

$$\phi \rightarrow \infty \quad (21)$$

This is the explanation of the absorption of electromagnetic radiation by an electron beam, i.e. when:

$$m = 9.10953 \times 10^{-31} \text{ kg} \quad (22)$$

$$c = 2.9979 \times 10^8 \text{ ms}^{-1} \quad (23)$$

$$h = 1.05459 \times 10^{-34} \text{ Js} \quad (24)$$

and when the Compton wavelength is:

$$\lambda = \frac{h}{mc} = 2.426309 \times 10^{-12} \text{ m} \quad (25)$$

The electron wavefunction is:

$$\phi = \phi_0 \exp\left(-i \frac{mc^2 z}{h}\right) \quad (26)$$

So absorption occurs when the electromagnetic wave number k is tuned to the wave number k_0 of the electron beam.

Therefore absorption can be understood as an Euler-Bernoulli resonance.

In three dimensions eq. (18) is:

$$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} + \frac{\partial^2 \phi}{\partial z^2} + k_0^2 \phi = A \cos(k_x x + k_y y + k_z z) \quad (27)$$

and eq. (27) can be solved by computer algebra.

From Eqs. (15) and (19):

$$\phi = \phi_0 \cos \kappa_0 Z = \frac{A \cos \kappa Z}{\kappa_0^2 - \kappa^2} \quad - (28)$$

for the electron wave function. Here ϕ is the electron potential, and κ is an electromagnetic wavenumber. Similarly, for the electron wave function:

$$\psi = \psi_0 \cos \kappa_0 Z = \frac{A \cos \kappa Z}{\kappa_0^2 - \kappa^2} \quad - (29)$$

Eqs. (28) and (29) are generally applicable resonance equations for the oscillation of any system with a small driving force.

For example, if an electromagnetic driving force is applied to a gravitational potential described by the gravitational ERE wave equation:

$$(\square + R)\Phi = 0 \quad - (30)$$

then

$$\Phi = \Phi_0 \cos \kappa_0 Z = \frac{A \cos \kappa Z}{\kappa_0^2 - \kappa^2} \quad - (31)$$

and counter gravitation occurs at:

$$\kappa_0 = \kappa. \quad - (32)$$

If the gravitational potential is assumed to be,

$$\begin{aligned} \Phi &= \Phi_0 \exp(-i \underline{\kappa} \cdot \underline{r}) = -\frac{MG}{r} \quad - (33) \\ &= \Phi_0 \cos \kappa_0 Z \end{aligned}$$

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$$\kappa_0 = \frac{1}{Z} \cos^{-1} \left(-\frac{mG}{\Phi_0 Z} \right) \quad - (34)$$

To estimate Φ_0 , we:

$$|\Phi| = \left(\Phi \cdot \Phi^* \right)^{1/2} = \frac{mG}{r} \quad - (35)$$

so

$$\Phi_0 = \left(\frac{mG}{r} \right) = \left(\frac{mG}{Z} \right)^{1/2} \quad - (36)$$

so

$$\kappa_0 = \frac{1}{Z} \cos^{-1} \left(-1 \right) \left(\frac{mG}{Z} \right) \quad - (37)$$

$$\boxed{\kappa_0 = \frac{\pi}{Z}} \quad - (38)$$

Resonance occurs when the electromagnetic κ is tuned to π/Z .

In three dimensions:

$$\begin{aligned} \Phi &= \Phi_0 \exp \left(-i(\kappa_x X + \kappa_y Y + \kappa_z Z) \right) \\ &= \frac{-mG}{(X^2 + Y^2 + Z^2)^{1/2}} \quad - (39) \end{aligned}$$