

312(7): Calculation of the Rest Frequency without Approximation for Monochromatic Radiation

The Beer Lambert law is:

$$\frac{\Phi}{\Phi_i} = \exp(-\alpha l) \quad - (1)$$

where

$$\Phi = \frac{\hbar (\omega^2 - \omega_0^2)^2}{3c^2 \pi^2 (e^{\beta} - 1)} \quad - (2)$$

and

$$\Phi_i = \frac{\hbar (\omega_i^2 - \omega_0^2)^2}{3c^2 \pi^2 (e^{\beta_i} - 1)} \quad - (3)$$

$$\text{So: } \frac{\omega^2 - \omega_0^2}{\omega_i^2 - \omega_0^2} = \left(\frac{e^{\beta} - 1}{e^{\beta_i} - 1} \right)^{1/2} \exp\left(-\frac{\alpha l}{2}\right) \quad - (4)$$
$$\therefore = A$$

$$\text{So: } \omega_0^2 = \frac{\omega^2 - A\omega_i^2}{1 - A} \quad - (5)$$

Various spectra and theories of the power absorption coefficient α can be used to evaluate ω_0^2 .
Note that ω_0^2 must be a constant.