

```
(%i1) kill(all);
(%o0) done
```

1 Eq.(1)

```
(%i1) ds2: c^2*dt^2-dr^2-r^2*dphi_1^2;
(ds2) -dphi_1^2 r^2 + c^2 dt^2 - dr^2

(%i2) dphi_1: dphi+omega*dt;
(dphi_1) dt ω + dphi
```

2 Eq.(4)

```
(%i3) ds2_a: ev(ds2);
(ds2_a) -(dt ω + dphi)^2 r^2 + c^2 dt^2 - dr^2
```

3 Eq.(6)

```
(%i4) ds2_b: (1-v^2/c^2)*(c^2*dt^2-2*r^2*Omega*dphi*dt)-(dr^2+r^2*dphi^2);
(ds2_b) (c^2 dt^2 - 2 Ω dphi dt r^2) (1 - v^2/c^2) - dphi^2 r^2 - dr^2

(%i5) Omega: omega*(1-v^2/c^2)^-1;
(Omega) ω / (1 - v^2/c^2)

(%i6) ev(ds2_b);
(%o6) (1 - v^2/c^2) (c^2 dt^2 - 2 dphi dt ω r^2 / (1 - v^2/c^2)) - dphi^2 r^2 - dr^2

(%i7) d: ratsimp(ev(ds2_a)-ev(ds2_b));
(d) dt^2 v^2 - dt^2 ω^2 r^2
```

3.1 with definition of omega from (8):

```
(%i8) ev(d, [v=omega*r]);
(%o8) 0
```

4 Einstein Metrics

```
(%i9) Delta_phi: 2*pi*(1/sqrt(m(r,t)-v^2/c^2)-1);
(Delta_phi) 2 π (1 / sqrt(m(r, t) - v^2/c^2) - 1)

(%i11) c: 1; v: 0.5;
(c) 1
(v) 0.5
```

Flat space

```
(%i13) m(r,t):=1;
D_phi_1: ev(Delta_phi);
(%o12) m(r, t):=1
(D_phi_1) 0.3094010767585034 π
```

Schwarzschild

```
(%i15) m(r,t):=1-1/r;
D_phi_2: ev(Delta_phi);
(%o14) m(r, t):=1 - 1/r
(D_phi_2) 2 π (1 / sqrt(0.75 - 1/r) - 1)
```

Kerr-Newman and Reissner-Nordstrom

```
(%i17) m(r,t):=1-1/r+1/r^2;
D_phi_3: ev(Delta_phi);
```

```
(%o16) m(r,t):=1-1/r+1/r^2
```

$$(D_phi_3) \quad 2\pi \left(\frac{1}{\sqrt{-\frac{1}{r} + \frac{1}{r^2} + 0.75}} - 1 \right)$$

Einstein-Rosen, Reissner-Weyl

```
(%i19) m(r,t):=1-1/r-1/r^2;
D_phi_4: ev(Delta_phi);
```

```
(%o18) m(r,t):=1-1/r-1/r^2
```

$$(D_phi_4) \quad 2\pi \left(\frac{1}{\sqrt{-\frac{1}{r} - \frac{1}{r^2} + 0.75}} - 1 \right)$$

Static de-Sitter

```
(%i21) m(r,t):=1-0.05*r^2;
D_phi_5: ev(Delta_phi);
```

```
(%o20) m(r,t):=1-0.05*r^2
```

$$(D_phi_5) \quad 2\pi \left(\frac{1}{\sqrt{0.75 - 0.05r^2}} - 1 \right)$$

```
(%i22) wxplot2d([D_phi_1,D_phi_2,D_phi_3,D_phi_4,D_phi_5], [r,0.,9], [y,0,15],
[legend, "Flat Space", "Schwarzschild",
"Kerr-Newman/Reissner-Nordstrom", "Einstein-Rosen/Reissner-Weyl",
"Static de-Sitter"])$
```

plot2d: expression evaluates to non-numeric value somewhere in plotting range.

plot2d: some values were clipped.

plot2d: expression evaluates to non-numeric value somewhere in plotting range.

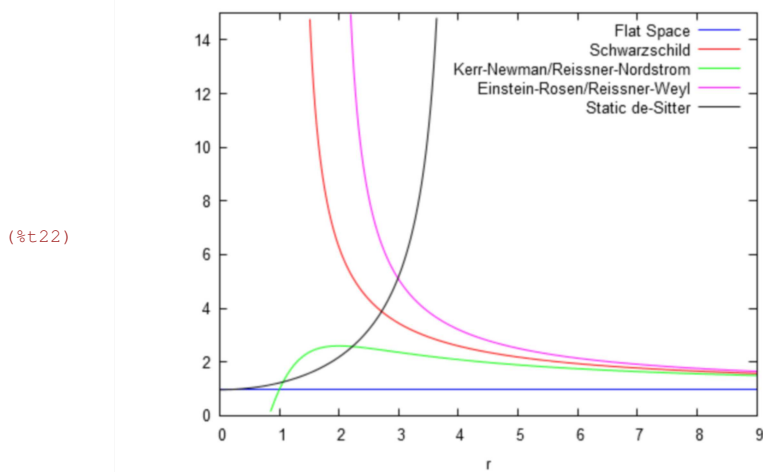
plot2d: some values were clipped.

plot2d: expression evaluates to non-numeric value somewhere in plotting range.

plot2d: some values were clipped.

plot2d: expression evaluates to non-numeric value somewhere in plotting range.

plot2d: some values were clipped.



```
(%i23) plot2d([D_phi_1,D_phi_2,D_phi_3,D_phi_4,D_phi_5], [r,0.,9], [y,0,15],  
[legend, "Flat Space", "Schwarzschild",  
"Kerr-Newman/Reissner-Nordstrom", "Einstein-Rosen/Reissner-Weyl",  
"Static de-Sitter"],  
[gnuplot_term, "png linewidth 2 font 'Arial' 16 size 800,600"],  
[gnuplot_out_file, "D:/Doc/Artikel-Eck/ECE-Theorie/Paper408/Fig1.png"])$
```

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