

DERIVATION OF THE DIRAC EQUATION, SIMPLE SUMMARY

Start with the definition of the 2×2 tetrad e^a_μ

$$\boxed{\gamma^a = e^a_\mu \gamma^\mu} \quad - (1)$$

where γ^a is a two-spinor in the tangent bundle and γ^μ a two-spinor in the Evans spacetime.

Thus:

$$\begin{bmatrix} \gamma^1 \\ \gamma^2 \end{bmatrix} = \begin{bmatrix} e^1_I & e^1_{II} \\ e^2_I & e^2_{II} \end{bmatrix} \begin{bmatrix} \gamma^I \\ \gamma^{II} \end{bmatrix} \quad - (2)$$

$$a = 1, 2; \quad \mu = I, II.$$

Form the column four vector or Evans spinor:

$$\psi = \begin{bmatrix} e^1_I \\ e^1_{II} \\ e^2_I \\ e^2_{II} \end{bmatrix}. \quad - (3)$$

The Evans wave equation states that:

$$(\square + kT) \gamma^a_\mu = 0. \quad - (4)$$

Therefore:

$$\boxed{(\square + kT) \psi = 0.} \quad - (5)$$

This is the Dirac equation in general relativity.

2) In the limit of special relativity the Evans
least curvature principle means that:

$$kT \rightarrow \left(\frac{mc}{\hbar} \right)^2 \quad - (6)$$

Finally the structure of eqn (5) becomes the
 structure of the Dirac equation of special relativity
 when:

$$\begin{bmatrix} \psi_I^I \\ \psi_{II}^I \\ \psi_{II}^I \\ \psi_{II}^I \end{bmatrix} \rightarrow \begin{bmatrix} \psi_{II}^R \\ \psi_{II}^R \\ \psi_{II}^L \\ \psi_{II}^L \end{bmatrix} = \begin{bmatrix} \phi^R \\ \phi^L \end{bmatrix} \quad - (7)$$

The Pauli spinors are:

$$\phi^R = \begin{bmatrix} \psi_{II}^R \\ \psi_{II}^R \end{bmatrix}; \quad \phi^L = \begin{bmatrix} \psi_{II}^L \\ \psi_{II}^L \end{bmatrix} \quad - (8)$$

and the Dirac spinor is:

$$\psi = \begin{bmatrix} \phi^R \\ \phi^L \end{bmatrix} \quad - (9)$$

The Dirac equation of special relativity is:

$$\left(\square + \left(\frac{mc}{\hbar} \right)^2 \right) \psi = 0 \quad - (10)$$

QED